

Real-time Bayesian Data Assimilation and Prediction for Livestock Epidemics

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- 1 Aims of model-based analysis
- 2 Application: Japan foot and mouth disease 2010
- 3 Epidemic model
- 4 Inference
- 5 Results

Aims

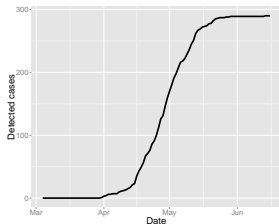
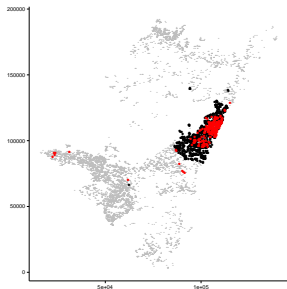
During an epidemic, we wish to use a model for...

- Nowcasting:
 - What is the current **extent** of the epidemic?
 - What puts a farm at **high risk**?
 - Is our **current control** strategy working?
- Forecasting:
 - Where will the disease go **next**?
 - What is the best control decision, given **imperfect knowledge**?

Japanese foot and mouth disease, 2010

Muroga *et al.* (2012)

- Miyazaki prefecture
- First detection late March 2010
- Day 0 = date of first detection
- 290 IPs
- 948 non-IP culls
- 10km vaccination implemented days 60–64
- DC culls mostly $>$ day 84



Nowcasting questions

At each stage of the epidemic:

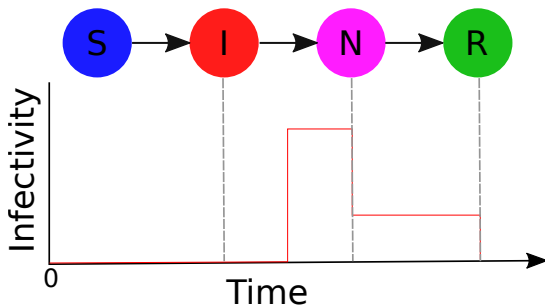
- Evaluate control policy
 - Vaccine efficacy
- What was the **true extent** of the outbreak?
 - Where are the undetected, or **occult** infections?
 - Vaccination strategy
 - Cull strategy
 - Target surveillance

Available data

I think like a statistician: data \implies model!

- Population data (explanatory variables):
 - Location of each farm: centroid, UTM coordinates
 - Number of cattle, pigs
 - Date of vaccination (∞ if not vaccinated)
- Epidemiological data (response variable(s)):
 - **Detection** (notification) date
 - **Cull** date
- **Infection** date not observed \implies **censored**

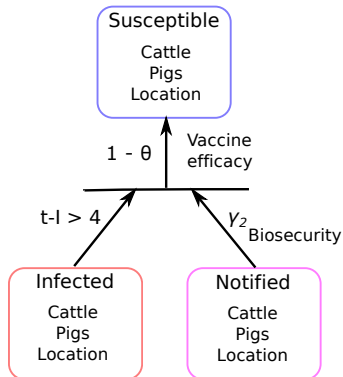
SINR model



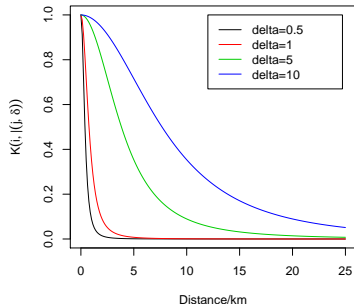
- Farm as epidemiological unit
- Infections determined by relationship to other **infectives**
- Infection times are **censored** (unobserved)
 - Undetected **occult** infections

Transmission model – quickly!

Keeling *et al.* 2001



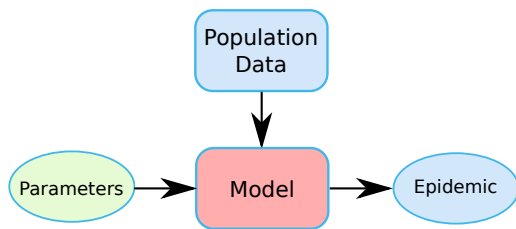
Spatial SINR Model



Spatial transmission
(proxy for network)

Model-based inference

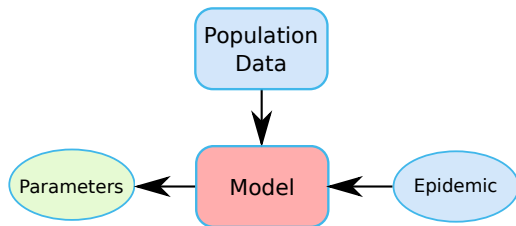
- Simulation moves **forward** in time
- Parameters **unknown**



- Prior to simulation, we need **parameter inference**

Inference

- Parameter inference looks **backward** in time
- Done in **real-time** during epidemic
- Inference requirements
 - Parameters estimated with full measurement of **uncertainty**
 - Account for **censored** and **occult** infection times
 - Easy to feed forward into **simulation**



Bayesian Inference

- ① Incorporation of **prior** information
- ② Machinery to account for **missing** data
 - Censored infection times
 - **occult** (undetected) infections
- ③ Fully likelihood-based
 - We know what we're getting from our model! (cf. ABC)
 - Likelihood **fast** to compute (cf. simulation)
 - GPU accelerated MCMC → results **overnight!**
- ④ Results provided as (posterior) **probability** distributions
 - Suitable for decision making under **uncertainty**
 - Don't be over-confident!

Vaccine efficacy

How effective was vaccination?

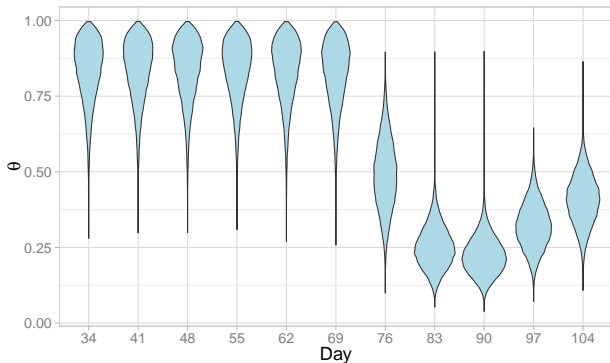
- Vaccine efficacy: θ parameter

$$s(j; t, \zeta, \phi) = (1 - \theta)^{[v_j < t]} \left(\tilde{c}_j^{\phi_c} + \zeta \tilde{p}_j^{\phi_p} \right)$$

- Vaccine efficacy tested 4, 8, 16 days post vaccination
- Results from weekly analyses during outbreak
- N.B. results from epidemic model avoids bias due to non-independence of infections

Vaccine efficacy

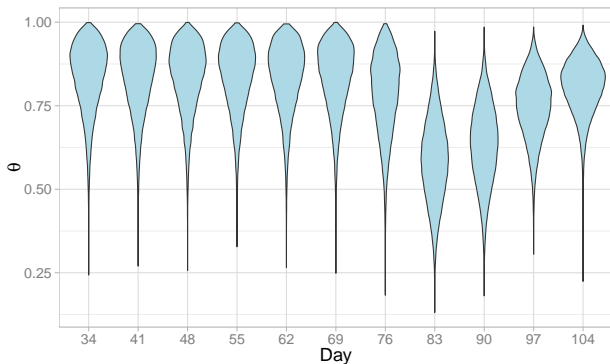
4 days post-vaccination



Efficacy 4 days post vaccination

Vaccine efficacy

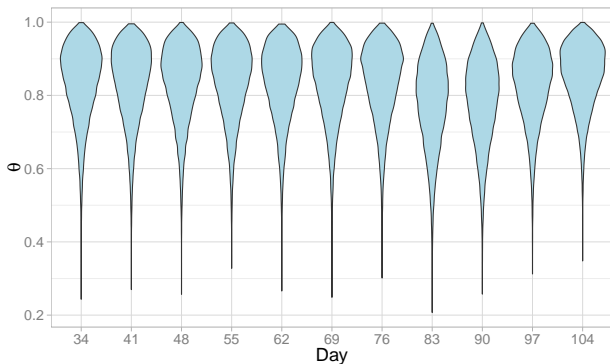
8 days post-vaccination



Efficacy 8 days post vaccination

Vaccine efficacy

14 days post-vaccination



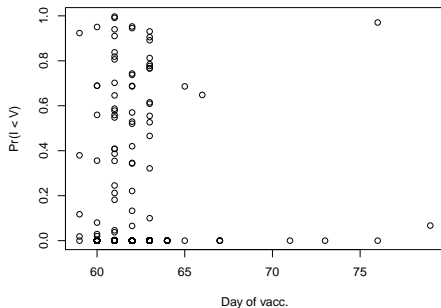
Efficacy 14 days post vaccination

Vaccination timing

- Was vaccination performed in time?

Vaccination timing

- Was vaccination performed in time?
- What was the probability that herds were **already infected** when they were vaccinated? (**Preliminary results!**)



Extent of the epidemic

- Was vaccination and/or DC culling keeping up with the epidemic?
- **Nowcasting** of undetected infections can tell us...

Show movie now...

Conclusions

Methods

- Likelihood-based inference is fast: **nowcast** information $\approx 1h$
 - Suitable for epidemic management *if* data comes in promptly!
 - Work on automated **data pipeline** to improve this
- Joint **parameter posterior** provides basis for **forecasting**
 - See Will Probert's talk up next...
- **GPU-enabled code** available at <http://fhm-chicas-code.lancs.ac.uk/groups/InFER/>
 - Help provided to compile and/or develop the model!

Conclusions

Japan 2010

- Apparent vaccine efficacy **highly sensitive** to delay between dose and immunity
 - Vaccine takes time to work – need to be **ahead** of the epidemic!
 - Eventual efficacy around 85%, but epidemic **escapes** vaccine delivery.
- Knowledge of spatial extent of the epidemic required
 - Optimise vaccine delivery, culling
 - Occult probabilities: prioritise active surveillance (see Jewell *et al* (2012) *Biostatistics*)
- More precise results: we need to to **negative** testing results as well as **positive**

The end

Transmission model – less quickly!

Susceptible → Infected

$$\lambda_{ij}(t) = \gamma_1 q(i; \xi, \psi) s(j; \zeta, \phi) K(i, j; \delta) \quad i \in \mathcal{I}, j \in \mathcal{S}$$

$$\lambda_{ij}^*(t) = \gamma_2 \beta_{ij}(t) \quad i \in \mathcal{N}, j \in \mathcal{S}$$

$$\epsilon_t = \begin{cases} \epsilon_1 & \text{if } t < \mu \\ \epsilon_1 \epsilon_2 & \text{otherwise} \end{cases}$$

$$q(i; t, \xi, \psi) = \mathbf{1}[t - li > 4] \left(\tilde{c}_i^{\psi_1} + \xi \tilde{p}_i^{\psi_p} \right)$$

$$s(j; t, \zeta, \phi) = (1 - \theta)^{\lfloor v_j < t \rfloor} \left(\tilde{c}_j^{\phi_c} + \zeta \tilde{p}_j^{\phi_p} \right)$$

\tilde{c}, \tilde{p} = cattle, pigs; ϵ_2 = movt ban; γ_2 = notification
 v = vaccine effect date; θ = farm-level vaccine efficacy